

# Disparate maturation adaptations to size-dependent mortality

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Body size is an important determinant of resource use, fecundity and mortality risk. Evolution of maturation size in response to size-dependent selection is thus a fundamental part of life-history theory. Increased mortality among small individuals has previously been predicted to cause larger maturation size, whereas increased mortality among large individuals is expected to have the opposite effect. Here we use a continuously size-structured model to demonstrate that, contrary to these widespread expectations, increased mortality among small individuals can have three alternative effects: maturation size may increase, decrease or become evolutionarily bistable. We show that such complex responses must be reckoned with whenever mortality is size-dependent, growth is indeterminate, reproduction impairs growth and fecundity increases with size. Predicting adaptive responses to altered size-dependent mortality is thus inherently difficult, since, as demonstrated here, such mortality cannot only reverse the direction of adaptation, but also cause abrupt shifts in evolutionarily stable maturation sizes.

**Keywords:** maturation size; size-dependent mortality; alternative equilibria; evolutionary bistability; adaptation; selection

## 1. INTRODUCTION

An individual's body size typically influences its fecundity, mortality and intra- and interspecific interactions. Adaptation of traits affecting body size in response to size-dependent selection pressures is thus a central topic in life-history theory (Roff 1992). It is also of practical importance, since size-dependent mortality occurs in many species, either naturally (Werner & Gilliam 1984) or induced by human exploitation (Law 2000). A key trait affecting body size is maturation size. Few evolutionary studies, however, have addressed maturation size directly and fewer still have examined its response to size-dependent mortality (Roff 1992). Most theoretical analyses have instead focussed on reproductive effort (Law 1979; Michod 1979) or energy allocation patterns (DeAngelis *et al.* 1985) or have analysed the effects of age- or stage-structured mortality, rather than of size-structured mortality (Schaffer & Rosenzweig 1977; Law 1979; Michod 1979; Roff 1981; Day *et al.* 2002). Existing evolutionary models of maturation size assessing size-dependent mortality predict that mortality among large individuals causes maturation size to decrease (Taylor & Gabriel 1992; Ernande *et al.* 2004), whereas mortality among small individuals is predicted to induce delayed maturation, at larger sizes (Taylor & Gabriel 1992). Both predictions have received empirical support (Edley & Law 1988; Reznick *et al.* 1990; Wellborn 1994; Haugen & Vollestad 2001; Johnson & Belk 2001). Thus, the effect of size-dependent mortality on the evolution of maturation size seems clear-cut. In particular, when maturation size is

the only evolving trait, its evolutionary response to size-dependent mortality appears to be uniquely determined.

In contrast, we show that mortality among small individuals has disparate effects on maturation size whenever mortality is size-dependent, growth is indeterminate, reproduction impairs growth and fecundity increases with size. We investigate a size-structured evolutionary model and show that the effect of mortality among small individuals on maturation size depends on how mortality varies with size, because the latter alters the trade-offs underlying maturation. Our results expose that predicting adaptive responses to size-dependent mortality, urgently needed, e.g. in fisheries (Law 2000), requires detailed knowledge of both natural mortality patterns and induced mortality. Such refined predictions are important since, as shown here, gradual changes in selection pressure can alter the direction of adaptation and cause abrupt shifts in evolutionarily stable maturation size.

## 2. MODEL

We consider an organism in which somatic growth is indeterminate and piecewise linear (e.g. some fish; Jørgensen 1992), reproduction reduces body growth, and all mature individuals reproduce. Size  $s$  is continuous and measured as body length. Individual growth rate  $g(s)$  for length  $s$  is then

$$g(s) = \begin{cases} g_i & s_0 < s \leq s_m, \\ g_m & s > s_m, \end{cases} \quad (2.1a)$$

where  $s_0$  is size at birth,  $s_m$  is size at maturation and  $g_i$  and  $g_m$  are the growth rates of immatures and matures, respectively. Owing to equation (2.1a), size at maturation,  $s_m$  and age at maturation,  $s_m/g_i$ , are strictly correlated traits, just representing two sides of the same coin.

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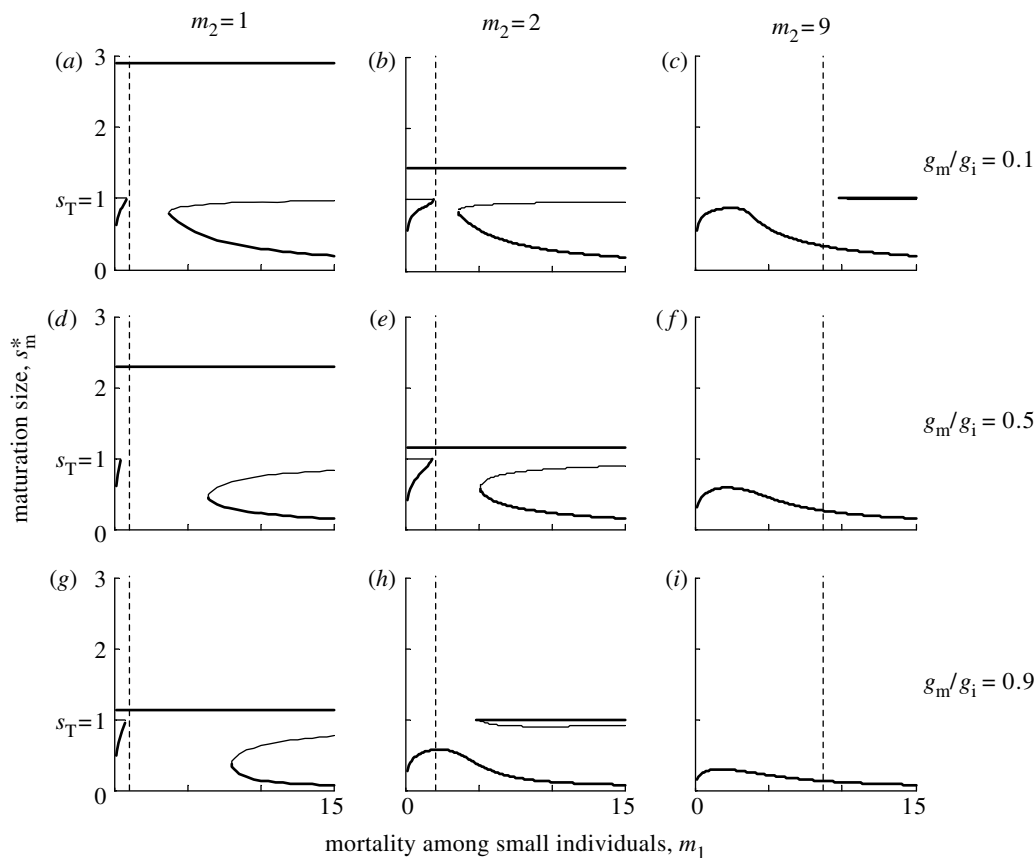


Figure 1. Evolutionarily stable maturation sizes  $s_m^*$  depend on mortality  $m_1$  among small individuals ( $s \leq s_T$ ), mortality  $m_2$  among large individuals ( $s > s_T$ ) and the relative growth rates  $g_m/g_i$  of mature individuals ( $s \geq s_m$ ) compared with immature individuals ( $s < s_m$ ). The effect of  $m_1$  on  $s_m^*$  (thick lines) and on evolutionarily unstable equilibria (thin lines) is shown in panels for three by three values of  $m_2$  and  $g_m/g_i$ . The vertical dashed lines in each panel indicate size-independent mortality,  $m_1 = m_2$ ; left of these lines we have  $m_1 < m_2$ , and right of these  $m_1 > m_2$ . Parameters:  $s_T = 1$  and  $g_i = 1$ . Note that parameters varied in this figure directly correspond to all three relevant dimensionless parameters of the model (see appendix). By measuring size and time in units of  $s_T$  and  $s_T/g_i$ , respectively, parameters used in this figure can be translated to particular systems.

Effective fecundity at size  $s$  is assumed to be proportional to weight, and thus to volume,

$$f(s) = bs^3, \tag{2.1b}$$

with scaling constant  $b$ . Note that effective fecundity measures the number of *viable* offspring, such that effects of parental size on, e.g. offspring survival soon after birth are accounted for.

We assume that mortality changes at threshold sizes  $s_L$  and  $s_T$ , such that

$$m(s) = \begin{cases} m_L & s_0 < s \leq s_L, \\ m_1 & s_L < s \leq s_T, \\ m_2 & s > s_T, \end{cases} \tag{2.1c}$$

i.e. small (large) individuals experience a (instantaneous) mortality  $m_1$  ( $m_2$ ). Since our focus is on size-dependent mortality, we avoid confounding its evolutionary effects by density-dependent mortality, by assuming that density regulation occurs through the mortality  $m_L$  of individuals ('larvae') too small ( $s \leq s_L$ ) ever to reproduce.

The dynamics of the density of individuals with size  $s > s_0$  at time  $t$  are given by (Metz & Dieckmann 1986)

$$\frac{\partial n(s, t)}{\partial t} = -\frac{\partial g(s)n(s, t)}{\partial s} - m(s)n(s, t), \tag{2.2a}$$

and the boundary condition

$$n(s_0, t) = g(s_0)^{-1} \int_{s_m}^{\infty} f(s)n(s, t) ds. \tag{2.2b}$$

We find evolutionarily stable and attainable equilibrium value(s) of maturation size,  $s_m^*$ , through evolutionary invasion analysis. When a variant with maturation size  $s'_m$  appears in a monomorphic resident population with maturation size  $s_m$ , the variant's fate is determined by its invasion fitness, i.e. by its exponential growth rate when rare in the resident population (Metz *et al.* 1992; Geritz *et al.* 1998). The invasion fitness is therefore given by the dominant Lyapunov exponent of the rare variant's (linear) dynamics. As Lyapunov exponents are difficult to calculate for infinite-dimensional dynamics arising in continuously structured populations we use the sign-equivalent proxy  $I$  of invasion fitness, based on the variant's lifetime reproductive success  $R_0$ ,

$$I(s'_m, s_m) = R_0 - 1 \\ = p_L(s_m)p_i(s'_m) \int_{s'_m}^{\infty} p_m(s'_m, s)f(s)g_m^{-1} ds - 1, \tag{2.3}$$

where  $p_L(s_m)$ ,  $p_i(s'_m)$  and  $p_m(s'_m, s)$  denote, respectively, the variant's probabilities of surviving the larval stage, the immature stage and from maturation to size  $s$  (see appendix). Since  $R_0 = 1$  and thus  $I = 0$ , always holds for

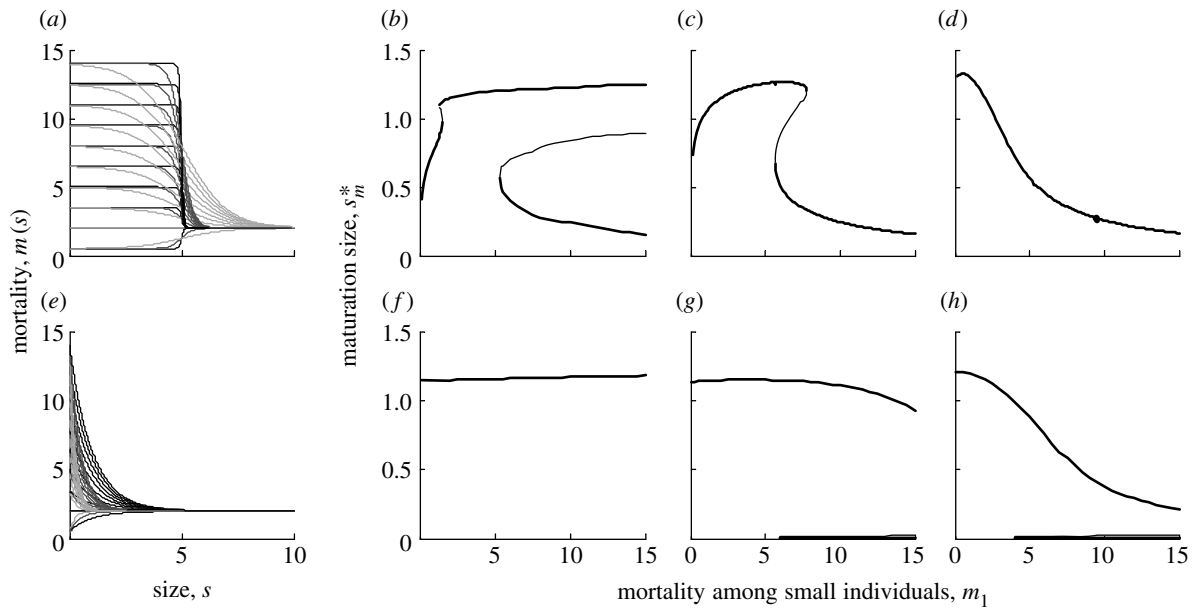


Figure 2. Disparate effects of mortality  $m_1$  among small individuals on maturation size  $s_m^*$  occur also when mortality is a continuous function of size. Leftmost panels (a, e) show three different shapes of size-dependent mortality for (a) when there is a threshold size for mortality,  $m(s) = m_2 + (m_1 - m_2)(1 - \tanh((s - s_T)/w))/(1 - \tanh(-s_T/w))$  and (e) without a threshold size,  $m(s) = m_2 + (m_1 - m_2)\exp(-s/s_T)$ . Panels (b-d, f-h) show the corresponding effects of  $m_1$  on  $s_m^*$ . Each set of curves in (a, e) corresponds to a different steepness of the mortality function (determined by  $w$  in (a) and by  $s_T$  in (e)) used in panels (b-d, f-h; steepness decreases from left to right across panels). Within each set of curves in (a, e), increasing  $m_1$  from bottom to top alters mortality from positively to negatively size-dependent (b-d, f-h). In (g) and (h), lower lines starting at  $m_1 = 6$  and  $m_1 = 4$ , respectively, depict a stable  $s_m^*$  and an unstable equilibrium in close proximity. Other symbols and parameters correspond to those used in figure 1e, with (b and black lines in a)  $w = 0.1$ , (c and dark grey lines in a)  $w = 0.5$ , (d and light grey lines in a)  $w = 2$ , (f and black lines in e)  $s_T = 0.25$ , (g and dark grey lines in e)  $s_T = 0.5$  and (h and light grey lines in e)  $s_T = 1$ .

the resident population at equilibrium,  $s'_m = s_m$ , it is evident that advantageous (deleterious) variants  $s'_m$  are characterized by  $I > 0$  ( $I < 0$ ).

### 3. RESULTS

Figure 1 shows that size-dependent mortality can have four different effects on maturation size. Mortality among small individuals can (i) increase maturation size, (ii) decrease it or (iii) cause two alternative stable maturation sizes to emerge (evolutionary bistability), whereas (iv) increased mortality among large individuals always decreases maturation size.

We now develop a mechanistic understanding of these findings. Disparate effects on maturation of mortality among small individuals occur because of three trade-offs, presented below, which emerge from three empirically well-justified assumptions: (i) somatic growth is reduced when reproducing, (ii) fecundity increases with size and (iii) mortality can be size-dependent:

— *Trade-off 1: fecundity versus juvenile mortality under size-independent mortality.* When mortality is size-independent ( $m_1 = m_2$ ), there is only one trade-off: whenever reproduction impairs growth and fecundity increases with size, this trade-off occurs between fecundity and the probability to survive until maturation. Individuals maturing at small sizes have lower fecundity than those maturing at larger sizes, but are more likely to survive until maturation ( $p_i$  decreases with  $s'_m$ , equation (A 2b)). Since growth is slower after maturation, any difference in fecundity at age between early- and late-maturing individuals will persist throughout life.

Increased size-independent mortality thus decreases maturation size (figure 1, compare thick curves at dashed vertical lines across panels).

When mortality depends on size, an additional trade-off emerges, the nature of which is determined by how mortality changes with size. There are two alternative options for this second trade-off.

— *Trade-off 2: fecundity versus juvenile and adult mortality under positively size-dependent mortality.* If mortality increases with size ( $m_1 < m_2$ ), the second trade-off occurs between fecundity and instantaneous mortality. Both the probabilities  $p_i$  and  $p_m$  to survive until and after maturation, respectively, then decrease with maturation size ( $p_i$  more so than when  $m_1 = m_2$ ; equation (A 2b)). When this effect is strong, i.e. when small individuals experience much less mortality than larger individuals, maturation size is much decreased. Thus, as mortality among small individuals increases at low levels, maturation size increases (figure 1, lower thick curves on the far left in all panels), before trade-off 1, above, takes over and decreases  $s_m^*$ . If overall mortality is sufficiently small, late maturation may be as beneficial as early maturation, and evolutionary bistability occurs, resulting in two alternative  $s_m^*$  (figure 1a,d, upper and lower thick curves in left part) separated by an unstable equilibrium (thin curves). This means that a population will evolve towards either smaller or larger  $s_m^*$ , depending on whether the initial maturation size lies below or above the unstable equilibrium. Note that, without the addition of extra frequency dependence (see appendix), the alternative

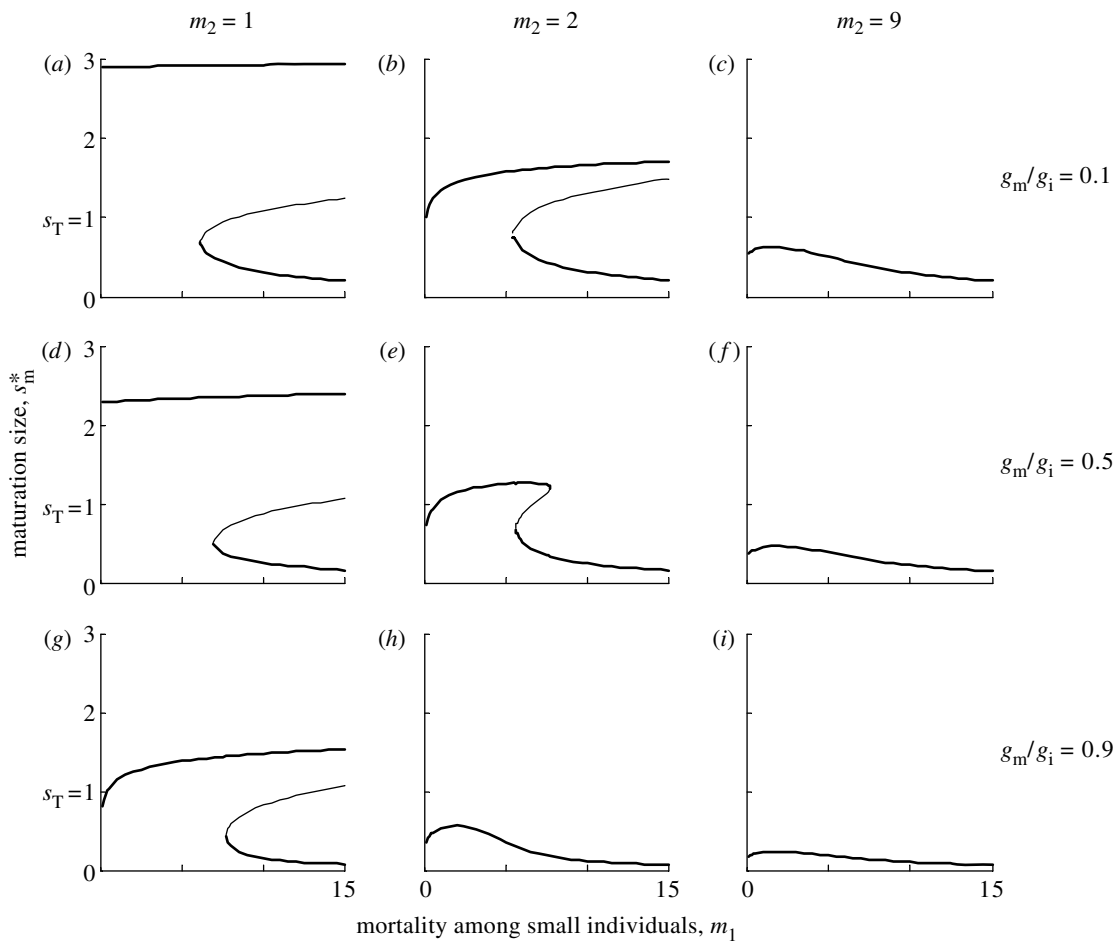


Figure 3. The effects of mortality  $m_1$  among small individuals on maturation size  $s_m^*$  when mortality is a continuous function of size,  $m(s) = m_2 + (m_1 - m_2)(1 - \tanh((s - s_T)/w))/(1 - \tanh(-s_T/w))$ , where  $w$  determines the steepness of the change in mortality with size occurring around  $s = s_T$ . Parameters and symbols as in figure 1, with  $w = 0.5$ .

$s_m^*$  are mutually exclusive, and evolutionary bistability thus cannot result in dimorphism.

— *Trade-off 3: juvenile versus adult mortality under negatively size-dependent mortality.* When mortality decreases with size ( $m_1 > m_2$ ) there is a ‘refuge’ from mortality at large body sizes ( $s > s_T$ ), and an alternative second trade-off emerges, now operating between survival until ( $p_i$ ) and after maturation ( $p_m$ ) for individuals maturing at small sizes (equations (A 2b,c)). These individuals have high  $p_i$ , but as reproduction impairs growth, they will take longer to grow to refuge size  $s_T$  beyond which mortality decreases (i.e.  $p_m$  is low). There are two solutions to this trade-off: individuals may either postpone reproduction until  $s_T$  (figure 1, upper thick curves in right part) or mature smaller than  $s_T$  (lower thick curves; this bistability occurs also in figure 1f,i, outside the illustrated range of  $m_1$ ). When mortality among small individuals increases, maturation below the size refuge becomes more beneficial, because the probability  $p_T$  to survive to the size refuge decreases (equation (A 3)). Thus, and also because of trade-off 1, the evolutionarily stable maturation size below the size refuge decreases (figure 1, lower thick curves in right part).

Mortality among large individuals decreases both the probability  $p_m$  to survive until maturation (for individuals maturing at sizes larger than  $s_T$ ; equation (A 2b)) and overall life expectancy. It therefore increases the

benefits of early maturation, and  $s_m^*$  decreases (figure 1, thick curves, across panels from left to right). Maturation size always decreases with increasing  $g_m/g_i$  (figure 1), because the growth cost of reproduction decreases. Note that the effect of  $m_1$  does not qualitatively depend on these costs:  $m_1$  can increase, decrease and cause evolutionary bistability of maturation size for any  $g_m/g_i$ .

These results are robust to variation in both parameters and type of size-dependent mortality. Our model has only three evolutionarily relevant parameters (see appendix), all varied in figure 1, which thus characterizes the model’s evolutionary behaviour exhaustively. Numerical analysis (see appendix) confirms that our conclusions extend to models in which the assumed discontinuity in size-dependent mortality (at  $s = s_T$ ) is smoothed (figures 2a–d and 3), and even to models without any threshold size for mortality (figures 2e–h and 4).

Disparate maturation effects are most pronounced when mortality changes steeply with size (figure 2). When mortality changes more gradually with size (large  $w$  in figure 2a–d or large  $s_T$  in figure 2e–h),  $m_1$  affects not only mortality at small sizes, but at most sizes (figure 2a,e). The parameter ranges for which  $m_1$  increases  $s_m^*$  or causes evolutionarily bistable maturation sizes are then much smaller (figure 2d,f–h) than when  $m_1$  predominantly affects mortality at small sizes (figures 1 and 2b,c). This is as expected: when  $m_1$  increases mortality at both small and large sizes, the probability to survive until maturation becomes very low for individuals postponing maturation

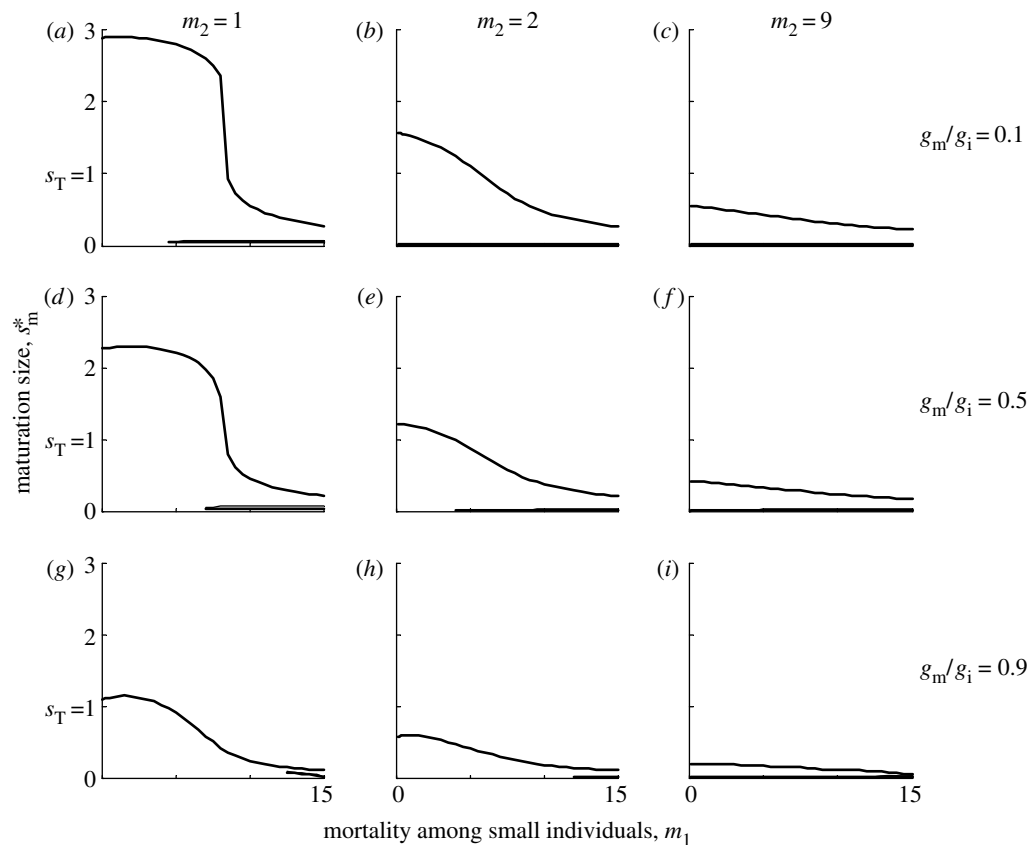


Figure 4. The effects of mortality  $m_1$  among small individuals on maturation size  $s_m^*$  when there is no threshold size for mortality,  $m(s) = m_2 + (m_1 - m_2)\exp(-s/s_T)$ . The lower lines in each panel depict a stable  $s_m^*$  and an unstable equilibrium in close proximity, other parameters and symbols as in figure 1.

until large sizes. As a result, bistability is then less frequent, and larger  $s_m^*$  disappear with increasing  $m_1$ .

#### 4. DISCUSSION

Previous life-history theory predicted that increased mortality among small individuals selects for delayed maturation (e.g. Taylor & Gabriel 1992), manifested either as an increased age or increased size at maturation. Here we have shown that, by contrast, such mortality can also decrease maturation size or cause evolutionary bistability, depending on how mortality changes with size. In fact, mortality among small individuals can only increase maturation size if mortality increases with size. Our results are original in a second regard: previous predictions of evolutionary bistability of maturation (Schaffer & Rosenzweig 1977; DeAngelis *et al.* 1985; Taborsky *et al.* 2003) all involved at least two evolving traits. By contrast, here we report evolutionary bistability when maturation size is the only evolving trait.

Disparate maturation responses to mortality among small individuals are expected in species with indeterminate growth and density-regulation early in life whenever (i) mortality depends on size, (ii) reproduction reduces body growth and (iii) fecundity increases with size—conditions that are widespread in nature (Roff 1992) and particularly common in fish (Wootton 1990). While the effect of mortality among large individuals in our model accords with earlier life-history theory (Taylor & Gabriel 1992; Ernande *et al.* 2004) and with empirical evidence (Edley & Law 1988; Wellborn 1994; Johnson & Belk

2001), previous models did not find disparate maturation responses to mortality among small individuals since either (a) one of the conditions (i) to (iii) was lacking, as in models where mortality is age- or stage-dependent rather than size-dependent (Law 1979; Michod 1979; Roff 1981; Day *et al.* 2002) or (b) disparate responses may have been overlooked (Taylor & Gabriel 1992; Takada & Caswell 1997; Nakaoka 1998). For example, evolutionary bistability is undetectable when optimal maturation size is assessed separately for maturation sizes smaller and larger than a size refuge from mortality, as in Takada & Caswell (1997). Alternatively, a focus on evolutionary effects other than those caused by variation in size-dependent mortality may have obscured the occurrence of the disparate responses documented here. For example, careful inspection of predicted maturation sizes in table 2 of Nakaoka (1998) reveals consistency with our findings (Nakaoka's analysis concentrated on the evolutionary effects of, in our notation, changes in  $s_T$  and  $m_2$ , and only investigated the case  $m_1 > m_2$ ).

Disparate responses of maturation size to mortality among small individuals are most pronounced when there is a size threshold to mortality (figures 1 and 2*a,b*) as, e.g. in species that can escape predation by outgrowing a vulnerable size range (Werner & Gilliam 1984). Nevertheless, disparate changes in maturation size are predicted also when mortality changes more gradually with size (figures 2*c,d* and 3). Even in complete absence of size thresholds, such as when mortality is an exponential function of size (figure 2*e*), mortality among small individuals can both elevate and depress maturation size,



as well as induce evolutionarily bistable maturation sizes (figures 2*f–h* and 4; Taborsky *et al.* 2003). Thus, the disparate maturation responses highlighted here are predicted to occur for several general types of size-dependent mortality.

The ubiquity of size-dependent mortality and the occurrence of size refuges from mortality (Werner & Gilliam 1984) suggest that disparate responses to mortality among small individuals may be a common phenomenon. Yet, empirical evidence of evolutionary responses available to date only confirms that such mortality can increase maturation size (Edley & Law 1988; Reznick *et al.* 1990; Haugen & Vollestad 2001). According to our results, this is expected when mortality increases with size, with the opposite response predicted when mortality decreases with size. In their experiments, Edley & Law (1988) and Reznick *et al.* (1990) compared two different selection regimes, but when applying high mortality among small individuals they simultaneously changed mortality from being positively to negatively size-dependent, which can either increase or decrease maturation size depending on relative mortalities in each selection regime (figure 1). In contrast, Haugen & Vollestad (2001) studied the selection pressure from harvesting of grayling, which changed over time but remained positively size-dependent. The increased maturation size they found thus accords with our predictions, whereas we are unaware of any experiment appropriate for testing our predicted adaptations to mortality among small individuals when mortality decreases with size.

The non-monotonic dependence of maturation size on mortality among small individuals reported here makes adaptive responses to increased mortality highly unpredictable in natural populations, for three reasons. First, gradual changes in mortality can abruptly increase stable maturation size whenever evolutionary bistability is lost (figure 1). Second, whenever alternative stable equilibria exist, adaptive responses to mortality changes depend on initial life histories (figure 1). Third, even in the absence of evolutionary bistability, a slight increase in mortality among small individuals can alter the direction of the adaptive response from gradually increasing to decreasing maturation size (figure 1). Acknowledging this complexity in adaptive responses to size-dependent mortality is crucial for improving the match between life-history theory and natural observations.

A case in point is evolutionary responses to fishing (Law 2000; Hutchings 2004). Fisheries may induce genetic changes in maturation (Olsen *et al.* 2004), with detrimental consequences for yield, stability and recovery potential of exploited stocks (Hutchings 2004). The extent of and remedies for such evolutionary changes are still uncertain. Our results show that suggested remedies, such as targeting only small individuals to reverse evolutionary changes induced by fishing (Conover & Munch 2002), may cause undesired effects by decreasing instead of increasing maturation size. According to our results, successful management of evolutionary responses by altering mortality among small individuals requires consideration of both pre-selection mortality patterns and the magnitude of mortality changes, in reflection of the complex evolutionary responses size-dependent mortality induces.

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## APPENDIX A

### (a) Resident equilibrium size structure

Below we explain results for  $s_m < s_T$ ; the opposite case is treated analogously. We obtain the equilibrium density distribution  $n^*(a)$  of resident individuals at age  $a$  from equations (2.1*a–c* and 2.2*a,b*). The resultant distribution is converted to the resident's equilibrium density distribution of sizes,  $n^*(s) = n^*(a)(\partial s(a)/\partial a)^{-1}$ , using equation (2.1*a*). Dividing  $n^*(s)$  by the total equilibrium population density  $N^*$ , we obtain the resident's equilibrium frequency distribution  $P^*(s)$  of sizes  $s$ ,

$P^*(s)$

$$= \begin{cases} g_1^{-1} \int_{s_m}^{\infty} f(\tilde{s}) P^*(\tilde{s}) d\tilde{s} \exp(-m_L^* g_1^{-1}(s_1 - s_0)) & s = s_L, \\ P^*(s_L) \exp(-m_1 g_1^{-1}(s - s_L)) & s_L < s \leq s_m, \\ P^*(s_m) g_1 g_m^{-1} \exp(-m_1 g_m^{-1}(s - s_m)) & s_m < s \leq s_T, \\ P^*(s_T) \exp(-m_2 g_m^{-1}(s - s_T)) & s > s_T, \end{cases} \quad (\text{A } 1)$$

where  $m_L^*$  is the density-dependent equilibrium mortality among individuals ('larvae') too small to ever reproduce; other parameters are as described in the main text. Relaxing the assumption that  $m_L$  acts uniformly throughout the larval stage does not alter the results qualitatively or quantitatively; neither does explicit modelling of growth between birth and  $s_L$ , nor varying  $s_L$  as such. In specific systems, the smallest possible maturation size  $s_L$  might be given by allometric constraints on, e.g. body cavity size. The only unknown remaining in equation (A 1), the resident's equilibrium probability of surviving the larval stage, is obtained from the first line of equation (A 1),

$$p_L(s_m) = \exp(-m_L^* g_1^{-1}(s_L - s_0)) = g_1 P^*(s_L) / \int_{s_m}^{\infty} f(s) P^*(s) ds.$$

This expression is further resolved in three steps by (i) using the third and fourth lines of equation (A 1) in the integral, (ii) using the second and third lines of equation (A 1) to replace  $P^*(s_m)$  and  $P^*(s_T)$  with expressions only involving  $P^*(s_L)$  and (iii) cancelling  $P^*(s_L)$ , which yields

$$\begin{aligned} p_L^{-1}(s_m) &= b g_m^{-1} \exp(-m_1 g_1^{-1}(s_m - s_L)) \left[ \int_{s_m}^{s_T} s^3 \exp(-m_1 g_m^{-1}(s - s_m)) ds \right. \\ &\quad \left. + \exp(-m_1 g_m^{-1}(s_T - s_m)) \int_{s_T}^{\infty} s^3 \exp(-m_2 g_m^{-1}(s - s_T)) ds \right]. \end{aligned} \quad (\text{A } 2a)$$

### (b) Variant survival probabilities

The variant's probability to survive the larval stage equals that of the resident (equation (A 2*a*)).

The variant's probability to survive the immature stage is

$$p_i(s'_m) = \begin{cases} \exp(-m_1 g_i^{-1}(s'_m - s_L)) & s'_m \leq s_T, \\ \exp(-m_1 g_i^{-1}(s_T - s_L) - m_2 g_i^{-1}(s'_m - s_T)) & s'_m \geq s_T. \end{cases} \quad (\text{A } 2b)$$

The variant's probability to survive from size  $s'_m$  to  $s$  is

$$p_m(s'_m, s) = \begin{cases} \exp(-m_1 g_m^{-1}(s - s'_m)) & s'_m \leq s \leq s_T, \\ \exp(-m_1 g_m^{-1}(s_T - s'_m) - m_2 g_m^{-1}(s - s_T)) & s'_m \leq s_T \leq s, \\ \exp(-m_2 g_m^{-1}(s - s'_m)) & s_T \leq s'_m \leq s. \end{cases} \quad (\text{A } 2c)$$

Inserting equations (A 2a–c) in equation (2.3) yields  $I$ . The result shows that  $I$  is independent of  $m_L$  and  $b$  and that the resident trait  $s_m$  affects  $R_0$  only multiplicatively through  $p_L(s_m)$ . Accordingly, selection on  $s_m$  is only trivially frequency-dependent (Heino *et al.* 1998), which means that neither evolutionary branching nor protected polymorphisms are possible and that all evolutionarily stable maturation sizes  $s_m^*$  are evolutionarily attainable (Meszéna *et al.* 2001). Equation (A 2a) shows that  $s_L$  has no bearing on the evolution of  $s_m$  (other than constraining it from below), since  $s_L$  (like  $s_m$ ) affects  $R_0$  in equation (2.3) only multiplicatively through  $p_L(s_m)$ : we thus assumed  $s_L = 0$  for simplicity.

The variant's probability to survive from size  $s_L$  to  $s$  is

$$p_T(s'_m) = \begin{cases} \exp(-m_1 g_i^{-1}(s'_m - s_L) - m_1 g_m^{-1}(s_T - s'_m)) & s'_m \leq s_T, \\ \exp(-m_1 g_i^{-1}(s_T - s_L)) & s'_m \geq s_T. \end{cases} \quad (\text{A } 3)$$

This extra result helps to appreciate trade-off 3, which emerges from the existence of a size refuge for  $s \geq s_T$  with  $m_1 > m_2$ .

**(c) Dimensionless analysis**

Our model features seven parameters:  $m_1, m_2, g_i, g_m, s_T, b$  and  $m_L$ . As shown above,  $b$  and  $m_L$  do not affect  $I$  and, thus, have no bearing on the evolution of  $s_m$ . A dimensionless version of our model follows from conveniently choosing the units in which we measure size and time, as  $s_T$  and  $s_T/g_i$ , respectively, resulting in three dimensionless parameters  $m_1 s_T/g_i, m_2 s_T/g_i$  and  $g_m/g_i$ . All of these are varied in figure 1, which thus characterizes the model exhaustively.

**(d) Continuous mortality functions**

To relax the assumption of discontinuous mortality with a sharp step at  $s = s_T$ , we considered the more general continuous function

$$m(s) = m_2 + (m_1 - m_2)(1 - \tanh((s - s_T)/w))/(1 - \tanh(-s_T/w)),$$

which results in a soft step around  $s = s_T$  (figure 2a) and which for  $w \rightarrow 0$  converges to the discontinuous mortality function used in figure 1 (figure 2a). Figure 3 shows the resultant effects of  $m_1$  on  $s_m^*$ , for the same values of  $m_2$  and  $g_m/g_i$  as used in figure 1.

As a further robustness test, we entirely relaxed the assumption of a threshold size in mortality by assuming that mortality is an exponential function of size,

$m(s) = m_2 + (m_1 - m_2)\exp(-s/s_T)$ , so that  $\partial^2 m(s)/\partial s^2$  had the same sign for all  $s$ . Note that here  $s_T$  no longer is a threshold parameter, but determines the size at which mortality drops to  $1/e = 36.8\%$  of its value at  $s = 0$ . Figure 4 shows the resultant effects of  $m_1$  on  $s_m^*$ , using the same parameter values as in figures 1 and 3.

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